| Parameter | Minimum value | Maximum value |
|--------------------|---------------|---------------|
| W | 10 mil | 30 mil |
| L | 40 mil | 60 mil |
| Н | 10 mil | 20 mil |
| \boldsymbol{e}_r | 8 | 10 |

TABLE I REGION OF INTEREST FOR THE MICROSTRIP LINE EXAMPLE

TABLE II THE SMSM AND FSMSM MAPPING PARAMETERS FOR THE MICROSTRIP TRANSMISSION LINE

| | SMSM | FSMSM |
|----|--|---|
| В | $\begin{bmatrix} 1.015 & -0.002 & -0.007 & -0.022 \\ -0.001 & 0.992 & 0.020 & 0.023 \\ -0.008 & 0.001 & 0.985 & 0.027 \\ 0.009 & -0.004 & 0.044 & 1.028 \end{bmatrix}$ | $\begin{bmatrix} 1.026 - 0.005 & 0.006 - 0.021 \\ -0.009 & 0.965 & -0.011 & 0.017 \\ -0.002 & 0.004 & 0.979 & 0.022 \\ 0.019 - 0.001 & 0.020 & 1.025 \end{bmatrix}$ |
| С | $[-0.011 - 0.008 \ 0.012 \ -0.036]^T$ | $\begin{bmatrix} -0.013 & 0.001 & 0.011 & -0.010 \end{bmatrix}^T$ |
| \$ | 0 (fixed) | $\begin{bmatrix} -0.006 & 0 & 0.002 & -0.002 \end{bmatrix}^T$ |
| t | 0 (fixed) | 0 |
| S | 1 (fixed) | 1.035 |
| d | 0 (fixed) | 0.001 |

TABLE III REGION OF INTEREST FOR THE MICROSTRIP RIGHT ANGLE BEND

| Parameter | Minimum value | Maximum value |
|--------------------|---------------|---------------|
| W | 20 mil | 30 mil |
| H | 8 mil | 16 mil |
| \boldsymbol{e}_r | 8 | 10 |

TABLE IV THE FSMSM MAPPING PARAMETERS FOR THE MICROSTRIP RIGHT ANGLE BEND

| | Gupta's model [11] | Jansen's model [12] |
|---|---|--|
| В | $\begin{bmatrix} 1.291 & 0.207 & 0.189 \\ 0.067 & 0.613 & -0.094 \\ 0.092 & -0.066 & 0.918 \end{bmatrix}$ | $\begin{bmatrix} 2.768 & 0.314 & 0.276 \\ -0.042 & 1.282 & 0.318 \\ -0.018 & -0.013 & 0.421 \end{bmatrix}$ |
| С | $\begin{bmatrix} 0.094 & -0.174 & 0.123 \end{bmatrix}^T$ | $\begin{bmatrix} 0.048 & -0.012 & 0.031 \end{bmatrix}^T$ |
| S | $\begin{bmatrix} 0.109 & -0.296 & 0.183 \end{bmatrix}^T$ | $\begin{bmatrix} 0.001 & -0.053 & 0.250 \end{bmatrix}^T$ |
| t | $[-0.001 - 0.002 - 0.002]^T$ | $[-0.001 - 0.002 - 0.001]^T$ |
| S | 3.269 | 2.343 |
| d | 0.019 | 0.015 |

TABLE V REGION OF INTEREST FOR THE MICROSTRIP STEP JUNCTION

| Parameter | Minimum value | Maximum value |
|--------------------|---------------|---------------|
| W_1 | 20 mil | 40 mil |
| W_2 | 10 mil | 20 mil |
| H | 10 mil | 20 mil |
| \boldsymbol{e}_r | 8 | 10 |

| TABLE VI |
|--------------------------------------|
| THE MSMDR MAPPING PARAMETERS FOR THE |
| MICROSTRIP STEP JUNCTION |

| | Target responses are | Target responses are |
|---|---|---|
| | $\{Im[S_{11}], Im[S_{21}], Im[S_{22}], Re[S_{21}]\}$ | $\{Re[S_{11}], Re[S_{22}]\}$ |
| В | $\begin{bmatrix} 0.764 & 0.033 & -0.062 & 0.074 \\ 0.191 & 0.632 & 0.255 & -0.502 \\ -0.023 & 0.116 & 1.485 & 0.018 \\ 0.676 & -0.365 & -0.111 & 0.177 \end{bmatrix}$ | $\begin{bmatrix} 3.071 & -0.008 & -0.010 & -0.004 \\ 0.008 & 0.202 & 0.032 & 0.004 \\ -0.001 & 0.001 & 1.152 & 0.000 \\ -0.077 & -0.118 & -0.002 & 1.241 \end{bmatrix}$ |
| с | $\begin{bmatrix} 0.002 & -0.002 & 0.002 & -0.006 \end{bmatrix}^T$ | $\begin{bmatrix} -0.001 & 0.001 & 0.000 & -0.003 \end{bmatrix}^T$ |
| S | $[-0.003 0.004 -0.001 -0.002]^T$ | 0 |
| t | $\begin{bmatrix} -0.001 & 0.000 & -0.005 & 0.000 \end{bmatrix}^T$ | $\begin{bmatrix} -0.001 & 0.000 & -0.007 & 0.003 \end{bmatrix}^T$ |
| S | 1.546 | 5.729 |
| d | 0.113 | 0.065 |

TABLE VII REGION OF INTEREST FOR THE MICROSTRIP SHAPED T-JUNCTION

| Parameter | Minimum value | Maximum value |
|--------------------|---------------|---------------|
| h | 15 mil | 25 mil |
| x | 5 mil | 15 mil |
| У | 5 mil | 15 mil |
| \boldsymbol{e}_r | 8 | 10 |

TABLE VIII THE MSMFI MAPPING PARAMETERS FOR THE MICROSTRIP SHAPED T-JUNCTION

| | 2 GHz to 16 GHz | 16 GHz to 20 GHz |
|---|--|--|
| В | $\begin{bmatrix} 1.04 & 0.07 & 0.01 & 0.08 & -0.06 & 0.00 & 0.22 \\ 0.00 & 0.89 & 0.00 & -0.07 & -0.20 & 0.06 & -0.03 \\ -0.00 & 0.07 & 0.99 & 0.04 & -0.12 & 0.01 & -0.06 \\ -0.04 & 0.00 & -0.01 & 0.97 & 0.10 & -0.06 & -0.27 \\ 0.01 & 0.04 & 0.00 & 0.03 & 0.99 & -0.05 & -0.03 \\ -0.13 & -0.05 & -0.04 & -0.16 & 0.12 & 0.99 & 0.62 \\ -0.08 & 0.12 & -0.03 & 0.00 & -0.07 & 0.03 & 0.83 \end{bmatrix}$ | $\begin{bmatrix} 0.99 & 0.02 - 0.00 & 0.01 - 0.09 - 0.01 & 0.13 \\ 0.05 & 0.85 & 0.01 - 0.07 - 0.28 & 0.01 - 0.01 \\ -0.06 & 0.15 & 0.98 & 0.04 - 0.25 & 0.00 & 0.02 \\ -0.10 - 0.06 - 0.03 & 0.88 & 0.13 - 0.09 - 0.27 \\ 0.08 & 0.04 & 0.03 & 0.11 & 1.07 - 0.04 - 0.12 \\ -0.14 - 0.02 - 0.05 - 0.15 & 0.23 & 1.03 & 0.51 \\ -0.13 & 0.22 - 0.04 & 0.02 - 0.07 & 0.03 & 0.87 \end{bmatrix}$ |
| с | $\begin{bmatrix} 0.02 & 0.01 & -0.01 & -0.03 & -0.01 & 0.07 & -0.03 \end{bmatrix}^T$ | $\begin{bmatrix} 0.01 & 0.01 & -0.01 & -0.03 & -0.01 & 0.05 & -0.03 \end{bmatrix}^T$ |
| S | $\begin{bmatrix} -0.01 & 0.09 & -0.10 & -0.02 & 0.00 & -0.02 & -0.20 \end{bmatrix}^T$ | $\begin{bmatrix} 0.00 & 0.01 & -0.01 & 0.00 & 0.00 & 0.00 & -0.02 \end{bmatrix}^T$ |
| t | 0 | $\begin{bmatrix} 0.01 & 0.00 & -0.02 & 0.00 & 0.00 & 0.00 \end{bmatrix}^T$ |
| S | 0.851 | 0.957 |
| d | -0.003 | 0.008 |



Fig. 1. The Frequency-Space Mapping Super Model (FSMSM) concept.



Fig. 2. The Space Mapping Super Model (SMSM) concept.



Fig. 3. The coarse model (a) and the enhanced coarse model (b).



Fig. 4. The Multiple Space Mapping for Device Responses (MSMDR).



Fig. 5. The Multiple Space Mapping for Frequency Intervals (MSMFI).



Fig. 6. Distribution of the base points in the region of interest for a 3-dimensional space [6].



Fig. 7. Microstrip line models: (a) the fine model; (b) the coarse model.



Fig. 8. Error in S₂₁ with respect to *em*TM: (a) by the microstrip transmission line model;
(b) by the microstrip transmission line SMSM; (c) by the microstrip transmission line FSMSM.



Fig. 9. Microstrip right angle bend: (a) the fine model; (b) the coarse model.



Fig. 10. Error in S_{11} of the microstrip right angle bend with respect to em^{TM} : (a) by Gupta's model [11]; (b) by Jansen's model [12].



Fig. 11. Error in S_{11} of the microstrip right angle bend with respect to em^{TM} : (a) by the enhanced Gupta's model [11]; (b) by the enhanced Jansen's model [12].



Fig. 12. Microstrip step junction.

Fig. 13. Error in S_{11} of the microstrip step junction with respect to em^{TM} : (a) before applying any modeling technique; (b) after applying FSMSM; (c) after applying the MSMDR algorithm.

Fig. 14. Error of the microstrip step junction coarse model with respect to em^{TM} : (a) in S_{11} ; (b) in S_{21} .

Fig. 15. Error of the microstrip step junction enhanced coarse model with respect to em^{TM} : (a) in S_{11} ; (b) in S_{21} .

Fig. 16. Histogram of the error in S_{21} of the microstrip step junction for 50 points in the region of interest at 40 GHz: (a) by the coarse model; (b) by the enhanced coarse model.

Fig. 17. Microstrip shaped T-junction: (a) the physical structure (fine model); (b) the coarse model.

Fig. 18. Responses of the shaped T-Junction at two test points in the region of interest by Sonnet's em (?), by the coarse model (---) and by the enhanced coarse model (?): (a) $|S_{11}|$; (b) $|S_{22}|$.

Fig. 21. Responses of the optimum shaped T-Junction by Sonnet's *em* (?), by the coarse model (---) and by the enhanced coarse model (?): (a) $|S_{11}|$; (b) $|S_{22}|$.