

# EM-Based Optimization Exploiting Partial Space Mapping and Exact Sensitivities

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**Abstract**—We present a family of robust techniques for exploiting sensitivities in electromagnetic (EM)-based circuit optimization through space mapping (SM) technology. We utilize derivative information for parameter extractions and mapping updates. We exploit a partial SM (PSM) concept, where a reduced set of parameters is sufficient for parameter extraction optimization. It reflects the idea of tuning and execution time is reduced. Upfront gradients of both EM (fine) model and coarse surrogates can initialize possible mapping approximations. We introduce several effective approaches for updating the mapping during the optimization iterations. Examples include the classical Rosenbrock function, modified to illustrate the approach, a two-section transmission-line 10:1 impedance transformer and a microstrip bandstop filter with open stubs.

**Index Terms**—CAD, design automation, electromagnetic (EM) simulation, EM optimization, microwave filters, optimization methods, space mapping.

## I. INTRODUCTION

USING an electromagnetic (EM) simulator (“fine” model) inside an optimization loop for the design process of microwave circuits can be prohibitive. Designers can overcome this problem by simplifying the circuit through circuit theory or by using the EM simulator with a coarser mesh. The space mapping (SM) approach [1], [2] relates a fine model to a physically based “coarse” surrogate. The fine model may be time intensive, field theoretic, and accurate, while the surrogate is a faster, circuit based, but less accurate, representation. SM introduces an efficient way to describe the relationship between the fine model and its surrogate. It makes effective use of the fast computation ability of the surrogate, on the one hand, and the accuracy of the fine model, on the other.

Surrogates in the context of filter design have been exemplified by Snel [3]. Practical benefits of empirical surrogates have also been demonstrated by Swanson and Wenzel [4]. They

achieved optimal mechanical adjustments by iterating between a finite element simulator and circuit simulator.

SM optimization involves the following steps. The “surrogate” is optimized to satisfy design specifications [5], thus providing the target response. A mapping is proposed between the parameter spaces of the fine model and its surrogate using a parameter extraction (PE) process. Then, an inverse mapping estimates the fine-model parameters corresponding to the (target) optimal surrogate parameters.

We present, for the first time, new techniques to exploit exact sensitivities in EM-based circuit design in the context of SM technology. If the EM simulator is capable of providing gradient information, these gradients can be exploited to enhance a coarse surrogate. New approaches for utilizing derivatives in the parameter extraction process and mapping update are presented.

We introduce also a new SM approach exploiting the concept of partial SM (PSM). Partial mappings were previously suggested in the context of neural space mapping [6]. Here, an efficient procedure exploiting a PSM concept is proposed. Several approaches for utilizing response sensitivities and PSM are suggested.

Exact sensitivities have been developed for nonlinear, harmonic-balance analyses [7], as well as implementable approximations such as the feasible adjoint sensitivity technique [8]. In the 1990s, Alessandri *et al.* spurred the application of the adjoint network method using a mode matching orientation [9]. Currently, we are developing the adjoint technique within a method of moments environment [10], [11]. These techniques facilitate powerful gradient-based optimizers. Our new work complements these efforts at gradient estimation for design optimization using EM simulations.

## II. AGGRESSIVE SPACE MAPPING

### A. Original Design Problem

The original design problem is

$$\mathbf{x}_f^* = \arg \min_{\mathbf{x}_f} U(\mathbf{r}_f(\mathbf{x}_f)). \quad (1)$$

Here, the fine-model response vector is denoted by  $\mathbf{r}_f \in \mathbb{R}^{m \times 1}$ , e.g.,  $|S_{11}|$  at selected frequency points, where  $m$  is the number of sample points. The fine-model point is denoted  $\mathbf{x}_f \in \mathbb{R}^{n \times 1}$ , where  $n$  is the number of design parameters.  $U$  is a suitable objective function. For example,  $U$  could be the minimax objective

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function with upper and lower specifications.  $\mathbf{x}_f^*$  is the optimal design to be determined.

### B. Parameter Extraction (PE)

PE is a crucial step in any SM algorithm. In PE, an optimization step is performed to extract a coarse-model point  $\mathbf{x}_c$  corresponding to the fine-model point  $\mathbf{x}_f$  that yields the best match between the fine model and its surrogate. The information stored in the design response  $\mathbf{r}_f$  may not be sufficient to describe the system under consideration properly. Thus, using only the design response in the PE may lead to nonuniqueness problems. Therefore, we need to obtain more information about the system and exploit it to extract the “best” coarse point and avoid nonuniqueness. For example, we may use responses such as real and imaginary parts of  $S$  parameters in the PE, even though we need only the magnitude of  $S_{11}$  to satisfy a certain design criterion. Now, we can assemble all the responses needed in the PE into one vector and define a new term, called a complete set of basic responses. The complete set of basic responses is designated by  $\mathbf{R}(\mathbf{x}) \in \mathfrak{R}^{M \times 1}$ , where  $M = mN_r$ ,  $m$  is the number of simulation frequency points, and  $N_r$  is the number of basic responses. In this context, the fine and its surrogate (coarse) responses are denoted by  $\mathbf{R}_f$  and  $\mathbf{R}_c$ , respectively. The traditional PE is described by the optimization problem

$$\mathbf{x}_c^{(j)} = \arg \min_{\mathbf{x}_c} \left\| \mathbf{R}_f(\mathbf{x}_f^{(j)}) - \mathbf{R}_c(\mathbf{x}_c) \right\|. \quad (2)$$

### C. Aggressive SM Approach

Aggressive SM solves the nonlinear system

$$\begin{aligned} \mathbf{f} &\triangleq \mathbf{P}(\mathbf{x}_f) - \mathbf{x}_c^* \\ &= \mathbf{x}_c - \mathbf{x}_c^* \\ &= \mathbf{0} \end{aligned} \quad (3)$$

for  $\mathbf{x}_f$ , where  $\mathbf{P}$  is a mapping defined between the two model spaces and  $\mathbf{x}_c \in \mathfrak{R}^{n \times 1}$  is the corresponding point in the coarse space,  $\mathbf{x}_c = \mathbf{P}(\mathbf{x}_f)$ . First-order Taylor approximations are given by

$$\mathbf{P}(\mathbf{x}_f) \approx \mathbf{P}(\mathbf{x}_f^{(j)}) + \mathbf{J}_P(\mathbf{x}_f^{(j)}) (\mathbf{x}_f - \mathbf{x}_f^{(j)}). \quad (4)$$

This can be described as

$$\mathbf{x}_c \approx \mathbf{x}_c^{(j)} + \mathbf{J}_P(\mathbf{x}_f^{(j)}) (\mathbf{x}_f - \mathbf{x}_f^{(j)}) \Big|_{\text{Through PE}} \quad (5)$$

where the Jacobian of  $\mathbf{P}$  at the  $j$ th iteration is expressed by

$$\mathbf{J}_P(\mathbf{x}_f^{(j)}) = \left( \frac{\partial \mathbf{P}^T}{\partial \mathbf{x}_f} \right)_{\mathbf{x}_f = \mathbf{x}_f^{(j)}}^T. \quad (6)$$

Equation (5) illustrates the nonlinearity of the mapping, where  $\mathbf{x}_c^{(j)}$  is related to  $\mathbf{x}_f^{(j)}$  through the PE process which is a non-

linear optimization problem. Recalling (4) and (5), we state a useful definition of the mapping Jacobian at the  $j$ th iteration

$$\mathbf{J}_P^{(j)} \triangleq \left( \frac{\partial (\mathbf{x}_c^{(j)T})}{\partial \mathbf{x}_f} \right) \Big|_{\text{PE}}^T. \quad (7)$$

We designate an approximation to this Jacobian by the square matrix  $\mathbf{B} \in \mathfrak{R}^{n \times n}$ , i.e.,  $\mathbf{B} \approx \mathbf{J}_P(\mathbf{x}_f)$ .

From (3) and (5), we can formulate the system

$$(\mathbf{x}_c^{(j)} - \mathbf{x}_c^*) + \mathbf{B}^{(j)} (\mathbf{x}_f^{(j+1)} - \mathbf{x}_f^{(j)}) = \mathbf{0} \quad (8)$$

which can be rewritten in the useful form

$$\mathbf{B}^{(j)} \mathbf{h}^{(j)} = -\mathbf{f}^{(j)}. \quad (9)$$

Solving (9) for  $\mathbf{h}^{(j)}$ , the quasi-Newton step in the fine space provides the next tentative iterate  $\mathbf{x}_f^{(j+1)}$

$$\mathbf{x}_f^{(j+1)} = \mathbf{x}_f^{(j)} + \mathbf{h}^{(j)}. \quad (10)$$

## III. PROPOSED ALGORITHMS

### A. PE Exploiting Sensitivity

We exploit the availability of the gradients of the fine model and surrogate responses to enhance the PE process. The Jacobian of the fine-model basic responses  $\mathbf{J}_f$  at  $\mathbf{x}_f$  and the corresponding Jacobian of the surrogate responses  $\mathbf{J}_c$  at  $\mathbf{x}_c$  can be obtained. Adjoint sensitivity analysis could be used to provide the exact derivatives, while finite differences are employed to estimate the derivatives if the exact derivatives are not available. Here, we present a new technique to formulate the PE to take into account not only the responses of the fine and its surrogate, but the corresponding gradients as well.

Through the traditional PE process, as in (2), we can obtain the point  $\mathbf{x}_c$  that corresponds to  $\mathbf{x}_f$ , such that

$$\mathbf{R}_f \approx \mathbf{R}_c. \quad (11)$$

Differentiating both sides of (11) with respect to  $\mathbf{x}_f$ , we obtain

$$\left( \frac{\partial \mathbf{R}_f^T}{\partial \mathbf{x}_f} \right)^T \approx \left( \frac{\partial \mathbf{R}_c^T}{\partial \mathbf{x}_c} \right)^T \left( \frac{\partial \mathbf{x}_c^T}{\partial \mathbf{x}_f} \right)^T. \quad (12)$$

Using (7), the relation (12) can be simplified to [12]

$$\mathbf{J}_f \approx \mathbf{J}_c \mathbf{B} \quad (13)$$

where  $\mathbf{J}_f$  and  $\mathbf{J}_c \in \mathfrak{R}^{M \times n}$ . Relation (13) assumes that  $\mathbf{J}_c$  is full rank and  $M \geq n$ , where  $M$  is the dimensionality of both  $\mathbf{R}_f$  and  $\mathbf{R}_c$ . Solving (13) for  $\mathbf{B}$  yields a least-squares solution [12]

$$\mathbf{B} = (\mathbf{J}_c^T \mathbf{J}_c)^{-1} \mathbf{J}_c^T \mathbf{J}_f. \quad (14)$$

At the  $j$ th iteration we obtain  $\mathbf{x}_c^{(j)}$  through a gradient parameter extraction (GPE) process. In GPE, we match not only the

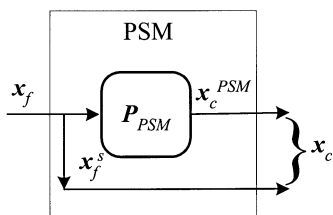


Fig. 1. Partial space mapping (PSM).

responses, but also the derivatives of both models through the optimization problem

$$\mathbf{x}_c^{(j)} = \arg \min_{\mathbf{x}_c} \left\| \begin{bmatrix} \mathbf{e}_0^T & \lambda \mathbf{e}_1^T & \cdots & \lambda \mathbf{e}_n^T \end{bmatrix}^T \right\|, \quad \lambda \geq 0 \quad (15)$$

where  $\lambda$  is a weighting factor,  $\mathbf{E} = [\mathbf{e}_1 \ \mathbf{e}_2 \ \dots \ \mathbf{e}_n]$ , and

$$\begin{aligned} \mathbf{e}_0 &= \mathbf{R}_f(\mathbf{x}_f^{(j)}) - \mathbf{R}_c(\mathbf{x}_c) \\ \mathbf{E} &= \mathbf{J}_f(\mathbf{x}_f^{(j)}) - \mathbf{J}_c(\mathbf{x}_c)\mathbf{B}. \end{aligned} \quad (16)$$

The nonuniqueness in the PE may lead to divergence or oscillatory behavior. Exploiting available gradient information enhances the uniqueness of the PE process. It also reflects the idea of multipoint extraction (MPE) [13], [14] in which simultaneous matching of a number of points of both spaces takes place.

### B. PSM

Utilizing a reduced set of the physical parameters of the coarse space might be sufficient to obtain an adequate surrogate for the fine model. A selected set of the design parameters are mapped onto the coarse space, and the rest of them ( $\mathbf{x}_f^s \subset \mathbf{x}_f$ ) are directly passed. The mapped coarse parameters are denoted by  $\mathbf{x}_c^{\text{PSM}} \in \mathbb{R}^{k \times 1}$ ,  $k \leq n$ , where  $n$  is the number of design parameters. PSM is illustrated in Fig. 1. It can be represented in the matrix form by

$$\mathbf{x}_c = \begin{bmatrix} \mathbf{x}_c^{\text{PSM}} \\ \mathbf{x}_f^s \end{bmatrix} = \begin{bmatrix} \mathbf{P}_{\text{PSM}}(\mathbf{x}_f) \\ \mathbf{x}_f^s \end{bmatrix}. \quad (17)$$

In this context, (13) becomes

$$\mathbf{J}_f \approx \mathbf{J}_c^{\text{PSM}} \mathbf{B}^{\text{PSM}} \quad (18)$$

where  $\mathbf{B}^{\text{PSM}} \in \mathbb{R}^{k \times n}$  and  $\mathbf{J}_c^{\text{PSM}} \in \mathbb{R}^{M \times k}$  is the Jacobian of the coarse model at  $\mathbf{x}_c^{\text{PSM}}$ . Solving (18) for  $\mathbf{B}^{\text{PSM}}$  yields the least-squares solution at the  $j$ th iteration

$$\mathbf{B}^{\text{PSM}(j)} = \left( \mathbf{J}_c^{\text{PSM}(j)T} \mathbf{J}_c^{\text{PSM}(j)} \right)^{-1} \mathbf{J}_c^{\text{PSM}(j)T} \mathbf{J}_f^{(j)}. \quad (19)$$

Relation (9) becomes underdetermined since  $\mathbf{B}^{\text{PSM}}$  is a fat rectangular matrix, i.e., the number of columns is greater than the number of rows. The minimum norm solution for  $\mathbf{h}^{(j)}$  is given by

$$\mathbf{h}_{\min \text{norm}}^{(j)} = \mathbf{B}^{\text{PSM}(j)T} \left( \mathbf{B}^{\text{PSM}(j)} \mathbf{B}^{\text{PSM}(j)T} \right)^{-1} \left( -\mathbf{f}^{(j)} \right). \quad (20)$$

The coarse-model parameters  $\mathbf{x}_c^{\text{PSM}}$  used in the PE can be determined by the sensitivity analysis proposed by Bandler *et al.*

[15]. It chooses the parameters that the coarse-model response is sensitive to.

### C. Mapping Update Alternatives

If we have exact derivatives of both the fine and coarse model, we can use them to obtain  $\mathbf{B}$  at each iteration using a least-squares solution as in (14). Note that this matrix can be iteratively fed back into the GPE process and refined before making a step in the fine-model space. We can also use (19) to update  $\mathbf{B}^{\text{PSM}}$ .

If we do not have exact derivatives, various approaches to initializing or constraining  $\mathbf{B}$  and  $\mathbf{B}^{\text{PSM}}$  can be devised; for example, we can use finite differences (perturbations). Either matrix may be updated using a Broyden update [16]. Hybrid schemes can be formally developed following the integrated gradient approximation approach to optimization by Bandler *et al.* [17]. One hybrid approach incorporates the use of perturbations and Broyden formula. Utilizing this approach reduces the effort of calculating exact derivatives. Perturbations are used to obtain an initial good approximation to  $\mathbf{B}$  and  $\mathbf{B}^{\text{PSM}}$  at the starting point. Then, the Broyden formula is used to update both matrices in the subsequent iterations.

On the assumption that the fine and coarse models share the same physical background, Bakr *et al.* [18] suggested that  $\mathbf{B}$  could be better conditioned, in the PE process, if it is constrained to be close to the identity matrix  $\mathbf{I}$  by

$$\mathbf{B} = \arg \min_{\mathbf{B}} \left\| \begin{bmatrix} \mathbf{e}_1^T \cdots \mathbf{e}_n^T \eta \Delta \mathbf{b}_1^T \cdots \eta \Delta \mathbf{b}_n^T \end{bmatrix}^T \right\|_2^2 \quad (21)$$

where  $\eta$  is a weighting factor and  $\mathbf{e}_i$  and  $\Delta \mathbf{b}_i$  are the  $i$ th columns of  $\mathbf{E}$  and  $\Delta \mathbf{B}$ , respectively, defined as

$$\begin{aligned} \mathbf{E} &= \mathbf{J}_f - \mathbf{J}_c \mathbf{B} \\ \Delta \mathbf{B} &= \mathbf{B} - \mathbf{I}. \end{aligned} \quad (22)$$

The analytical solution of (21) is given by

$$\mathbf{B} = \left( \mathbf{J}_c^T \mathbf{J}_c + \eta^2 \mathbf{I} \right)^{-1} \left( \mathbf{J}_c^T \mathbf{J}_f + \eta^2 \mathbf{I} \right). \quad (23)$$

### D. Proposed Algorithms

#### Algorithm 1 Full Mapping/GPE/Jacobian update

**Step 1** Set  $j = 1$ . Initialize  $\mathbf{B} = \mathbf{I}$  for the PE process. Obtain the optimal coarse-model design  $\mathbf{x}_c^*$  and use it as the initial fine-model point

$$\mathbf{x}_f^{(1)} = \mathbf{x}_c^* = \arg \min_{\mathbf{x}_c} U(\mathbf{r}_c(\mathbf{x}_c)). \quad (24)$$

*Comment* Minimax optimization is used to obtain the optimal coarse solution.

**Step 2** Execute a preliminary GPE step as in (15).

*Comment* Match the responses and the corresponding gradients.

**Step 3** Refine the mapping matrix  $\mathbf{B}$  using Jacobians (14).

*Comment* A least-squares solution is used to refine a square matrix  $\mathbf{B}$  using Jacobians.

**Step 4** Stop if

$$\left\| \mathbf{f}^{(j)} \right\| \leq \varepsilon_1 \text{ or } \left\| \mathbf{R}_f^{(j)} - \mathbf{R}_c^* \right\| \leq \varepsilon_2. \quad (25)$$

*Comment* Loop until the stopping conditions are satisfied.

**Step 5** Solve (9) for  $\mathbf{h}^{(j)}$ .

**Step 6** Find the next  $\mathbf{x}_f^{(j+1)}$  using (10).

**Step 7** Perform GPE as in (15).

**Step 8** Update  $\mathbf{B}^{(j)}$  using (14).

*Comment* A least-squares solution is used to update  $\mathbf{B}$  at each iteration exploiting Jacobians.

**Step 9** Set  $j = j + 1$  and go to Step 4.

#### Algorithm 2 Partial SM/GPE/Jacobian update

**Step 1** Set  $j = 1$ . Initialize  $\mathbf{B}^{\text{PSM}} = [\mathbf{I}^{\text{PSM}} \mathbf{0}]$  for the PE process. Obtain the optimal coarse-model design  $\mathbf{x}_c^*$  and use it as the initial fine-model point as in (24).

**Step 2** Execute a preliminary GPE step as in (15).

**Step 3** Refine the mapping matrix  $\mathbf{B}^{\text{PSM}}$  using (19).

*Comment* A least-squares solution is used to refine a rectangular matrix  $\mathbf{B}^{\text{PSM}}$  using Jacobians.

**Step 4** Stop if (25) holds.

*Comment* Loop until the stopping conditions are satisfied.

**Step 5** Evaluate  $\mathbf{h}^{(j)}$  using (20).

*Comment* A minimum norm solution for a quasi-Newton step  $\mathbf{h}^{(j)}$  in the fine space is used.

**Step 6** Find the next  $\mathbf{x}_f^{(j+1)}$  using (10).

**Step 7** Perform GPE as in (15).

**Step 8** Use (19) to update  $\mathbf{B}^{\text{PSM}(j)}$ .

*Comment* A least-squares solution is used to update  $\mathbf{B}^{\text{PSM}}$  at each iteration.

**Step 9** Set  $j = j + 1$  and go to Step 4.

#### Algorithm 3 Partial SM/PE/Hybrid approach for mapping update

**Step 1** Set  $j = 1$ . Initialize  $\mathbf{B}^{\text{PSM}} = [\mathbf{I}^{\text{PSM}} \mathbf{0}]$  for the PE process. Obtain the optimal coarse-model design  $\mathbf{x}_c^*$  and use it as the initial fine-model point as in (24).

**Step 2** Execute a preliminary traditional PE step as in (2).

**Step 3** Refine the mapping matrix  $\mathbf{B}^{\text{PSM}}$  using (19).

*Comment* A least-squares solution is used to refine a rectangular matrix  $\mathbf{B}^{\text{PSM}}$  using Jacobians.

**Step 4** Stop if (25) holds.

*Comment* Loop until the stopping conditions are satisfied.

**Step 5** Evaluate  $\mathbf{h}^{(j)}$  using (20).

**Step 6** Find the next  $\mathbf{x}_f^{(j+1)}$  using (10).

**Step 7** Perform traditional PE as in (2).

**Step 8** Update  $\mathbf{B}^{\text{PSM}(j)}$  using a Broyden formula.

*Comment* A hybrid approach is used to update  $\mathbf{B}^{\text{PSM}}$ .

**Step 9** Set  $j = j + 1$  and go to Step 4.

The output of the algorithms is the fine space mapped optimal design  $\bar{\mathbf{x}}_f$  and the mapping matrix  $\mathbf{B}$  (Algorithm 1) or  $\mathbf{B}^{\text{PSM}}$  (Algorithms 2 and 3).

## IV. EXAMPLES

### A. Rosenbrock Banana Problem [12], [19]

Test problems based on the classical Rosenbrock banana function are studied. We let the original Rosenbrock function

$$R_c = 100(x_2 - x_1^2)^2 + (1 - x_1)^2 \quad (26)$$

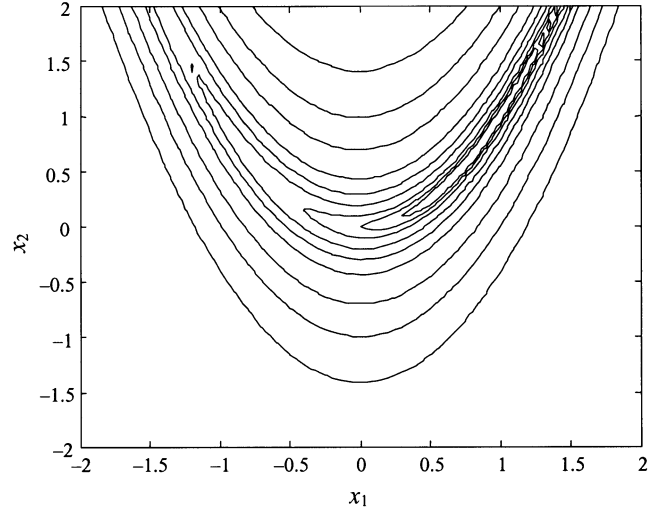


Fig. 2. Contour plot of the “coarse” original Rosenbrock banana function.

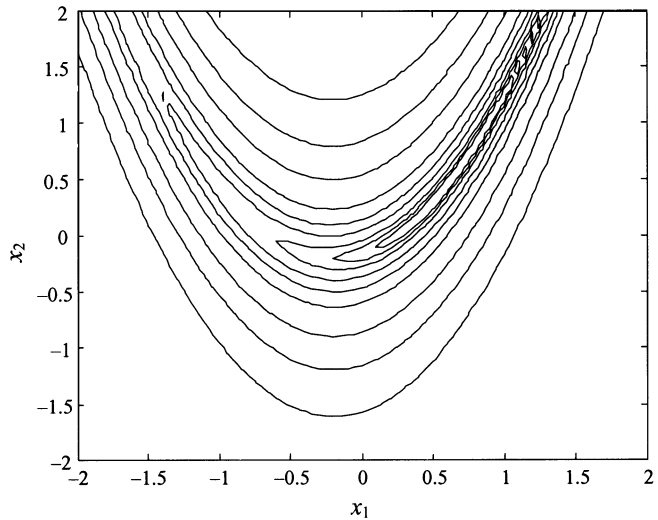


Fig. 3. Contour plot of the “fine” shifted Rosenbrock banana function.

be a “coarse” model. The optimal solution is  $\mathbf{x}_c^* = [1.0 \ 1.0]^T$ . A contour plot is shown in Fig. 2.

*Case 1: Shifted Rosenbrock Problem:* We propose a “fine” model as a shifted Rosenbrock function

$$R_f = 100((x_2 + \alpha_2) - (x_1 + \alpha_1)^2)^2 + (1 - (x_1 + \alpha_1))^2 \quad (27)$$

where

$$\boldsymbol{\alpha} = \begin{bmatrix} \alpha_1 \\ \alpha_2 \end{bmatrix} = \begin{bmatrix} -0.2 \\ 0.2 \end{bmatrix}. \quad (28)$$

The optimal fine-model solution is  $\mathbf{x}_f^* = \mathbf{x}_c^* - \boldsymbol{\alpha} = [1.2 \ 0.8]^T$  (see Fig. 3 for a contour plot).

We apply Algorithm 1. Exact “Jacobians”  $\mathbf{J}_f$  and  $\mathbf{J}_c$  are used in the GPE process and in mapping update. The algorithm converges in one iteration to the exact solution (see Table I).

*Case 2: Transformed Rosenbrock Problem:* A “fine” model is described by the transformed Rosenbrock function

$$R_f = 100(u_2 - u_1^2)^2 + (1 - u_1)^2 \quad (29)$$

TABLE I  
“SHIFTED” ROSENBOCK BANANA PROBLEM

Iteration	$\mathbf{x}_c^{(j)}$	$f^{(j)}$	$\mathbf{B}^{(j)}$	$\mathbf{h}^{(j)}$	$\mathbf{x}_f^{(j)}$	$R_f^{(j)}$
0	$\begin{bmatrix} 1.0 \\ 1.0 \end{bmatrix}$	---	---	---	$\begin{bmatrix} 1.0 \\ 1.0 \end{bmatrix}$	31.4
1	$\begin{bmatrix} 0.8 \\ 1.2 \end{bmatrix}$	$\begin{bmatrix} -0.2 \\ 0.2 \end{bmatrix}$	$\begin{bmatrix} 1.0 & 0.0 \\ 0.0 & 1.0 \end{bmatrix}$	$\begin{bmatrix} 0.2 \\ -0.2 \end{bmatrix}$	$\begin{bmatrix} 1.2 \\ 0.8 \end{bmatrix}$	0
	$\begin{bmatrix} 1.0 \\ 1.0 \end{bmatrix}$	$\begin{bmatrix} 0 \\ 0 \end{bmatrix}$				

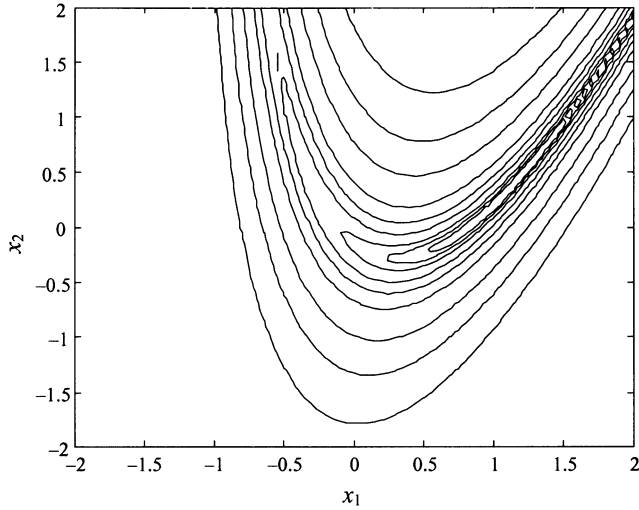


Fig. 4. Contour plot of the “fine” transformed Rosenbrock banana function.

where

$$\mathbf{u} = \begin{bmatrix} 1.1 & -0.2 \\ 0.2 & 0.9 \end{bmatrix} \mathbf{x} + \begin{bmatrix} -0.3 \\ 0.3 \end{bmatrix}. \quad (30)$$

The exact solution evaluated by the inverse transformation is  $\mathbf{x}_f^* = [1.2718447 \ 0.4851456]^T$  to seven decimals. A contour plot is shown in Fig. 4. Applying Algorithm 1, we get a solution, to a very high accuracy, in six iterations (see Table II for details).

### B. Capacitively Loaded 10:1 Impedance Transformer [20]

We apply Algorithm 2 to a two-section transmission line (TL) 10:1 impedance transformer. We consider a “coarse” model as an ideal two-section TL, where the “fine” model is a capacitively loaded TL with capacitors  $C_1 = C_2 = C_3 = 10$  pF. The fine and coarse models are shown in Figs. 5 and 6, respectively. Design parameters are normalized lengths  $L_1$  and  $L_2$ , with respect to the quarter-wave length  $L_q$  at the center frequency 1 GHz, and characteristic impedances  $Z_1$  and  $Z_2$ . Normalization makes the problem well posed. Thus,  $\mathbf{x}_f = [L_1 \ L_2 \ Z_1 \ Z_2]^T$ . Design specifications are

$$|S_{11}| \leq 0.5, \quad \text{for } 0.5 \text{ GHz} \leq \omega \leq 1.5 \text{ GHz}$$

with 11 points per frequency sweep. We utilize the real and imaginary parts of  $S_{11}$  in the GPE (15). The fine and surrogate responses can be easily computed as a function of the design parameters using circuit theory [21]. We solve (15) using the

TABLE II  
“TRANSFORMED” ROSENBOCK BANANA PROBLEM

Iteration	$\mathbf{x}_c^{(j)}$	$f^{(j)}$	$\mathbf{B}^{(j)}$	$\mathbf{h}^{(j)}$	$\mathbf{x}_f^{(j)}$	$R_f^{(j)}$
0	$\begin{bmatrix} 1.0 \\ 1.0 \end{bmatrix}$	---	---	---	$\begin{bmatrix} 1.0 \\ 1.0 \end{bmatrix}$	108.3
1	$\begin{bmatrix} 0.526 \\ 1.384 \end{bmatrix}$	$\begin{bmatrix} -0.474 \\ 0.384 \end{bmatrix}$	$\begin{bmatrix} 1.01 & -0.05 \\ 0.01 & 1.01 \end{bmatrix}$	$\begin{bmatrix} 0.447 \\ -0.385 \end{bmatrix}$	$\begin{bmatrix} 1.447 \\ 0.615 \end{bmatrix}$	5.119
2	$\begin{bmatrix} 1.185 \\ 1.178 \end{bmatrix}$	$\begin{bmatrix} 0.185 \\ 0.178 \end{bmatrix}$	$\begin{bmatrix} 0.96 & -0.13 \\ -0.096 & 1.06 \end{bmatrix}$	$\begin{bmatrix} -0.218 \\ -0.187 \end{bmatrix}$	$\begin{bmatrix} 1.23 \\ 0.427 \end{bmatrix}$	4.4E-3
3	$\begin{bmatrix} 0.967 \\ 0.929 \end{bmatrix}$	$\begin{bmatrix} -0.033 \\ -0.071 \end{bmatrix}$	$\begin{bmatrix} 1.09 & -0.19 \\ 0.168 & 0.92 \end{bmatrix}$	$\begin{bmatrix} 0.0429 \\ 0.0697 \end{bmatrix}$	$\begin{bmatrix} 1.273 \\ 0.497 \end{bmatrix}$	1.8E-6
4	$\begin{bmatrix} 1.001 \\ 1.001 \end{bmatrix}$	$\begin{bmatrix} 0.001 \\ 0.001 \end{bmatrix}$	$\begin{bmatrix} 1.10001 & -0.1999 \\ 0.1999 & 0.9001 \end{bmatrix}$	$\begin{bmatrix} -0.001 \\ -0.002 \end{bmatrix}$	$\begin{bmatrix} 1.2719 \\ 0.4952 \end{bmatrix}$	5E-10
5	$\begin{bmatrix} 1.00002 \\ 1.00004 \end{bmatrix}$	$\begin{bmatrix} 0.2\text{E}-4 \\ 0.4\text{E}-4 \end{bmatrix}$	$\begin{bmatrix} 1.1 & -0.2 \\ 0.2 & 0.9 \end{bmatrix}$	$\begin{bmatrix} 0.3\text{E}-4 \\ 0.5\text{E}-4 \end{bmatrix}$	$\begin{bmatrix} 1.2718 \\ 0.4951 \end{bmatrix}$	3E-17
6	$\begin{bmatrix} 1.0 \\ 1.0 \end{bmatrix}$	$\begin{bmatrix} 0.1\text{E}-8 \\ 0.3\text{E}-8 \end{bmatrix}$	$\begin{bmatrix} 1.1 & -0.2 \\ 0.2 & 0.9 \end{bmatrix}$	$\begin{bmatrix} 0.2\text{E}-8 \\ 0.3\text{E}-8 \end{bmatrix}$	$\mathbf{x}_f^*$	9E-29

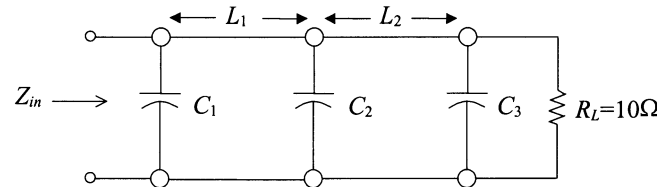


Fig. 5. Two-section impedance transformer: “fine” model.

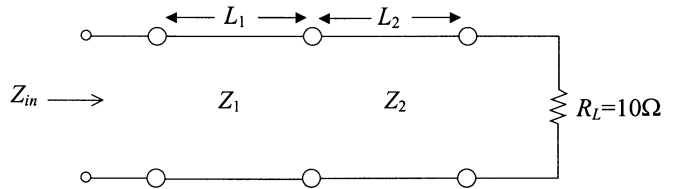


Fig. 6. Two-section impedance transformer: “coarse” model.

TABLE III  
COARSE MODEL SENSITIVITIES WITH RESPECT TO THE DESIGN PARAMETERS FOR THE CAPACITIVELY LOADED IMPEDANCE TRANSFORMER

Parameter	$\hat{S}_i$
$L_1$	0.98
$L_2$	1.00
$Z_1$	0.048
$Z_2$	0.048

Levenberg–Marquardt algorithm for nonlinear least-squares optimization available in the Matlab Optimization Toolbox [22].

*Case 1:* Based on a sensitivity analysis [15] for the design parameters of the coarse model shown in Table III we note that the normalized lengths  $[L_1 \ L_2]$  are the key parameters. Thus, we consider  $\mathbf{x}_c^{\text{PSM}} = [L_1 \ L_2]^T$ , while  $\mathbf{x}_f^* = [Z_1 \ Z_2]^T$  are kept fixed at the optimal values, i.e.,  $Z_1 = 2.23615 \ \Omega$  and  $Z_2 = 4.47230 \ \Omega$ . We employ adjoint sensitivity-analysis techniques [23] to obtain the exact Jacobians of the fine and coarse models. We initialize  $\mathbf{B}^{\text{PSM}}$  by using the Jacobian information of both models at the starting point as in (19). The algorithm converges in a single iteration (two fine-model evaluations). The corresponding responses are illustrated in Figs. 7 and 8, respec-

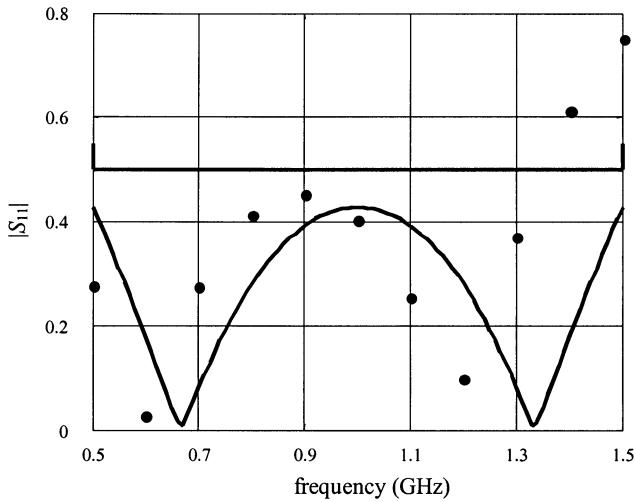


Fig. 7. Optimal coarse-model target response (—) and the fine-model response at the starting point (●) for the capacitively loaded 10:1 transformer with  $L_1$  and  $L_2$  as the PSM coarse-model parameters.

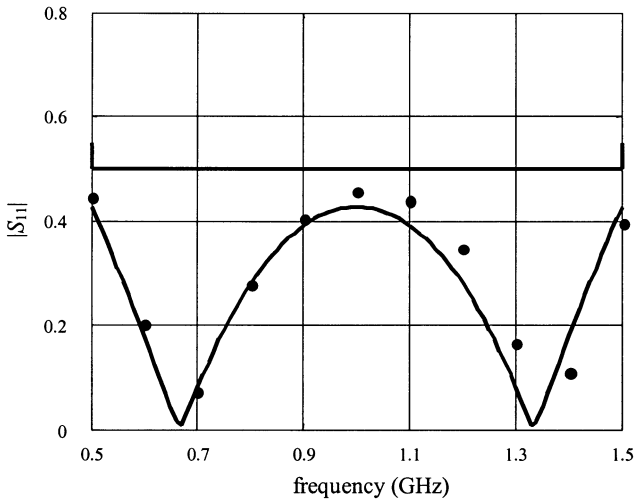


Fig. 8. Optimal coarse-model target response (—) and the fine-model response at the final design (●) for the capacitively loaded 10:1 transformer with  $L_1$  and  $L_2$  as the PSM coarse-model parameters.

tively. The final mapping is

$$\mathbf{B}^{\text{PSM}} = \begin{bmatrix} 1.075 & 0.087 & 0.006 & 0.002 \\ 0.049 & 1.139 & -0.008 & 0.006 \end{bmatrix}.$$

This result confirms the sensitivity analysis presented in Table III. It supports our decision of taking into account only  $[L_1 L_2]$ , represented by the first and the second columns in  $\mathbf{B}^{\text{PSM}}$ , as design parameters. As is well known, the effect of the capacitance in the fine model can only be substantially compensated by a change of the length of a TL. Therefore, changes of  $[Z_1 Z_2]$  hardly affect the final response.

The reduction of  $\|\mathbf{x}_c - \mathbf{x}_c^*\|_2$  versus iteration is shown in Fig. 9. The reduction of the objective function  $U$  in Fig. 10 also illustrates convergence (two iterations).

*Case 2:* We apply Algorithm 2 for  $\mathbf{x}_c^{\text{PSM}} = [L_1]$ . The result is similar to Fig. 8. Convergence is in a single iteration (two

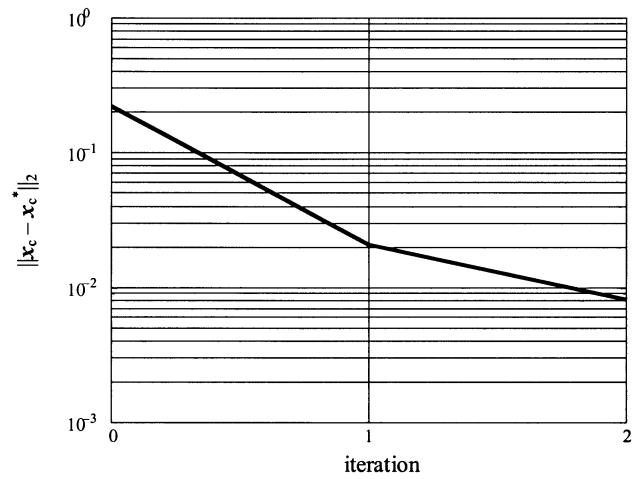


Fig. 9.  $\|\mathbf{x}_c - \mathbf{x}_c^*\|_2$  versus iteration for the capacitively loaded 10:1 transformer with  $L_1$  and  $L_2$  as the PSM coarse-model parameters.

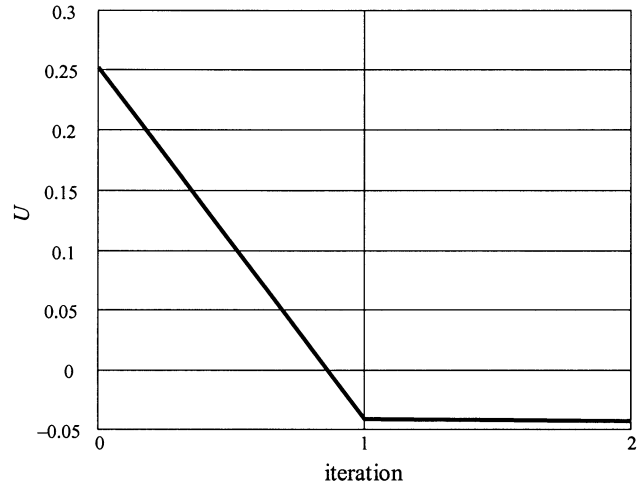


Fig. 10.  $U$  versus iteration for the capacitively loaded 10:1 transformer with  $L_1$  and  $L_2$  as the PSM coarse-model parameters.

fine-model evaluations). The final mapping is

$$\mathbf{B}^{\text{PSM}} = [1.371 \quad 0.909 \quad 0.0033 \quad 0.0055].$$

As we can see, changes in  $[L_1]$  represented by the first element in  $\mathbf{B}^{\text{PSM}}$  are significant. However, the second parameter  $[L_2]$  is affected also. This arises from the fact that  $[L_1 L_2]$  have the same physical effect; namely, that of length in a TL.

*Case 3:* We apply Algorithm 2 for  $\mathbf{x}_c^{\text{PSM}} = [L_2]$ . The result is similar to Fig. 8 and it converges in a single iteration (two fine-model evaluations). The final mapping is

$$\mathbf{B}^{\text{PSM}} = [0.8989 \quad 1.186 \quad -0.0043 \quad 0.0087].$$

As in case 2, changes in one parameter,  $[L_2]$  in this case, have a dominant role. This affects  $[L_1]$ , the parameter which shares the same physical nature.

The initial and final designs for all three cases are shown in Table IV. We realize that the algorithm aims to rescale the TL lengths to match the responses in the PE process (see Fig. 7). In

TABLE IV  
 INITIAL AND FINAL DESIGNS FOR THE CAPACITIVELY LOADED  
 IMPEDANCE TRANSFORMER

Parameter	$\mathbf{x}_f^{(0)}$	$\mathbf{x}_f^{(1)}$ ( $L_1$ and $L_2$ )	$\mathbf{x}_f^{(1)}$ ( $L_1$ )	$\mathbf{x}_f^{(1)}$ ( $L_2$ )
$L_1$	1.0	0.8995	0.8631	0.8521
$L_2$	1.0	0.8228	0.9126	0.8259
$Z_1$	2.23615	2.2369	2.2352	2.2365
$Z_2$	4.47230	4.4708	4.4716	4.4707

$L_1$  and  $L_2$  are normalized lengths  
 $Z_1$  and  $Z_2$  are in ohm

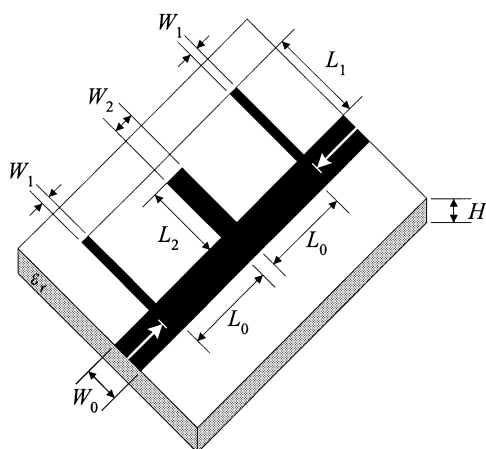


Fig. 11. Bandstop microstrip filter with open stubs: “fine” model.

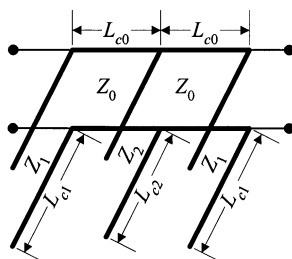


Fig. 12. Bandstop microstrip filter with open stubs: “coarse” model.

all cases, both  $[L_1 \ L_2]$  are reduced by similar overall amounts, as expected.

By carefully choosing a reduced set of design parameters, we can affect other “redundant” parameters and the overall circuit response as well, which implies the idea of tuning. Nevertheless, the use of the entire set of design parameters should give the best result.

### C. Bandstop Microstrip Filter With Open Stubs [6]

Algorithm 3 is applied to a symmetrical bandstop microstrip filter with three open stubs. The open-stub lengths are  $L_1$ ,  $L_2$ ,  $L_1$  and the corresponding stub widths are  $W_1$ ,  $W_2$ ,  $W_1$ . An alumina substrate with thickness  $H = 25$  mil, width  $W_0 = 25$  mil, dielectric constant  $\epsilon_r = 9.4$ , and loss tangent = 0.001

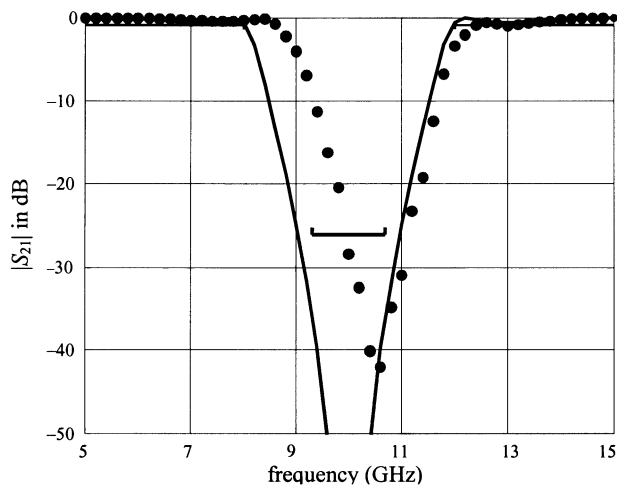

 Fig. 13. Optimal OSA90/hope coarse target response (—) and *em* fine-model response at the starting point (•) for the bandstop microstrip filter using a fine frequency sweep (51 points) with  $L_1$  and  $L_2$  as the PSM coarse-model parameters.

 TABLE V  
 COARSE-MODEL SENSITIVITIES WITH RESPECT TO DESIGN PARAMETERS  
 FOR THE BANDSTOP MICROSTRIP FILTER

Parameter	$\hat{S}_i$
$W_1$	0.065
$W_2$	0.077
$L_0$	0.677
$L_1$	1.000
$L_2$	0.873

is used for a 50- $\Omega$  feeding line. The design parameters are  $\mathbf{x}_f = [W_1 \ W_2 \ L_0 \ L_1 \ L_2]^T$ . The design specifications are

$$|S_{21}| \leq 0.05 \text{ for } 9.3 \text{ GHz} \leq \omega \leq 10.7 \text{ GHz}$$

$$|S_{21}| \geq 0.9 \text{ for } 12 \text{ GHz} \leq \omega \text{ and } \omega \leq 8 \text{ GHz.}$$

Sonnet’s *em* [24] driven by Empipe [25] is employed as the fine model, using a high-resolution grid with a 1 mil  $\times$  1 mil cell size. As a coarse model, we use simple TLs for modeling each microstrip section and classical formulas [21] to calculate the characteristic impedance and the effective dielectric constant of each TL. It is seen that  $L_{c2} = L_2 + W_0/2$ ,  $L_{c1} = L_1 + W_0/2$ , and  $L_{c0} = L_0 + W_1/2 + W_2/2$ . We use OSA90/hope [25] built-in TL elements TRL. The fine model and its surrogate coarse model are illustrated in Figs. 11 and 12, respectively.

Using OSA90/hope, we can get the optimal coarse solution at 10 GHz as  $\mathbf{x}_c^* = [4.560 \ 9.351 \ 107.80 \ 111.03 \ 108.75]^T$  (in mils). We use 21 points per frequency sweep. The coarse- and fine-model responses at the optimal coarse solution are shown in Fig. 13 (fine sweep is used only for illustration). We utilize the real and imaginary parts of  $S_{11}$  and  $S_{21}$  in the traditional PE. Sensitivity analysis for the coarse model is given in Table V. During the PE, we consider  $\mathbf{x}_c^{\text{PSM}} = [L_1 \ L_2]^T$  while  $\mathbf{x}_f^* = [W_1 \ W_2 \ L_0]^T$  are held fixed at the optimal coarse solution. Finite differences estimate the fine and coarse

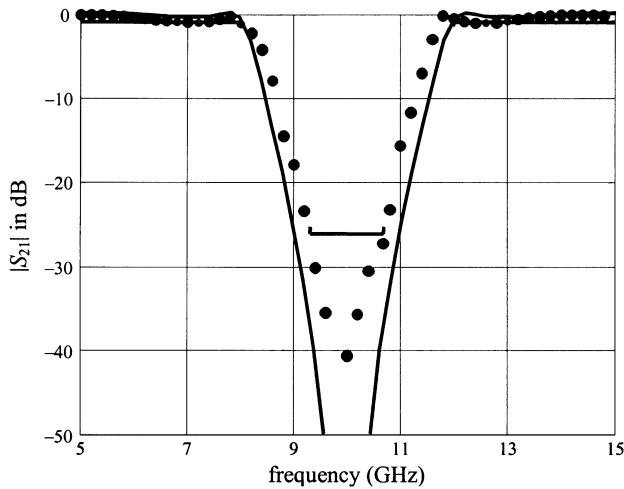


Fig. 14. Optimal OSA90/hope coarse target response (—) and *em* fine-model response at the final design (●) for the bandstop microstrip filter using a fine frequency sweep (51 points) with  $L_1$  and  $L_2$  as the PSM coarse-model parameters.

Jacobians used to initialize  $B^{\text{PSM}}$ , as in (19). A hybrid approach is used to update  $B^{\text{PSM}}$  at each iteration.

Algorithm 3 converges in five iterations. The PE execution time for the whole process is 59 min on an IBM-IntelliStation<sup>1</sup> machine. The optimal coarse-model response and the final design fine response are depicted in Fig. 14. The convergence of the algorithm is depicted in Fig. 15, where the reduction of  $\|\mathbf{x}_c - \mathbf{x}_c^*\|_2$  versus iteration is illustrated. The initial and final design values are shown in Table VI. The final mapping is given by

$$B^{\text{PSM}} = \begin{bmatrix} 0.570 & 0.168 & 0.209 & 0.911 & 0.214 \\ -0.029 & 0.154 & 0.126 & -0.024 & 0.470 \end{bmatrix}.$$

We notice that  $[L_1 \ L_2]$ , represented by the last two columns, are dominant parameters.

We run Algorithm 3 using all design parameters in the PE and in calculating the quasi-Newton step in the fine space, i.e., we use a full mapping. The algorithm converges in five iterations, however, the PE process takes 75 min on an IBM-IntelliStation<sup>1</sup> machine. The initial and final designs are given in Table VII. The final mapping is

$$B = \begin{bmatrix} 0.532 & -0.037 & 0.026 & 0.017 & -0.006 \\ -0.051 & 0.543 & 0.022 & -0.032 & 0.026 \\ 0.415 & 0.251 & 1.024 & 0.073 & 0.011 \\ 0.169 & -0.001 & -0.022 & 0.963 & 0.008 \\ -0.213 & -0.003 & -0.045 & -0.052 & 0.958 \end{bmatrix}.$$

The reduction of  $\|\mathbf{x}_c - \mathbf{x}_c^*\|_2$  versus iteration is shown in Fig. 16.

The notion of tuning is evident in this example also, where the various lengths and widths which constitute the designable parameters (see Fig. 11) have obvious physical interrelations.

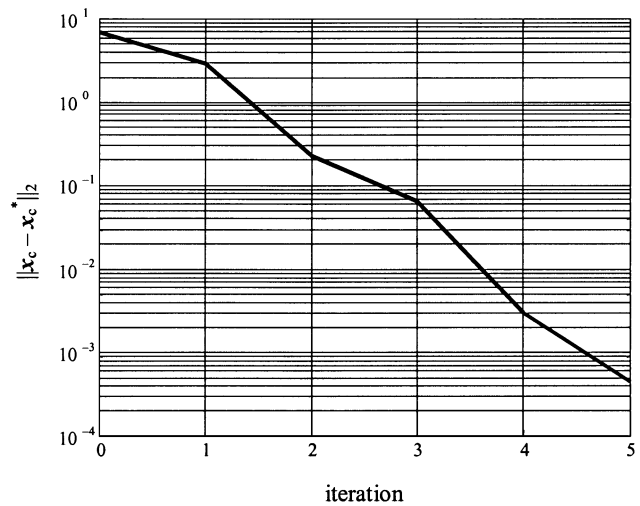


Fig. 15.  $\|\mathbf{x}_c - \mathbf{x}_c^*\|_2$  versus iteration for the bandstop microstrip filter using  $L_1$  and  $L_2$  as the PSM coarse-model parameters.

TABLE VI  
INITIAL AND FINAL DESIGNS FOR THE BANDSTOP MICROSTRIP FILTER USING  $L_1$  AND  $L_2$

Parameter	$\mathbf{x}_f^{(0)}$	$\mathbf{x}_f^{(5)}$
$W_1$	4.560	7.329
$W_2$	9.351	10.672
$L_0$	107.80	109.24
$L_1$	111.03	115.53
$L_2$	108.75	111.28

All values are in mils

TABLE VII  
INITIAL AND FINAL DESIGNS FOR THE BANDSTOP MICROSTRIP FILTER USING A FULL MAPPING

Parameter	$\mathbf{x}_f^{(0)}$	$\mathbf{x}_f^{(5)}$
$W_1$	4.560	8.7464
$W_2$	9.351	19.623
$L_0$	107.80	97.206
$L_1$	111.03	116.13
$L_2$	108.75	113.99

All values are in mils

#### D. Comparison With Previous Approaches

All SM-based algorithms, by their very nature, are expected to produce acceptable designs in a small number of fine-model evaluations, typically 3–10. Hence, a basis for comparison must be simplicity, ease of programming, robustness on many examples and, in particular, avoidance of designer intervention. Our extensive convergence results (Tables I and II, Figs. 9, 10, 15, and 16) of our gradient-based proposal demonstrate that we averted false parameter extractions, do not require sophisticated programming, and do not rely on designer intervention.

<sup>1</sup>AMD Athlon, 400 MHz.



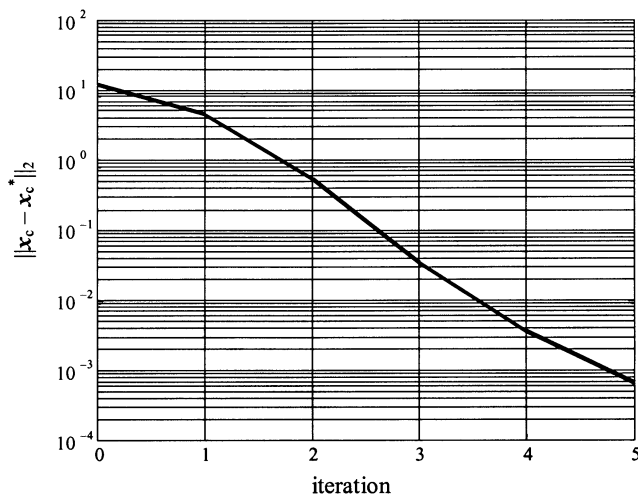


Fig. 16.  $\|x_c - x_c^*\|_2$  versus iteration for the bandstop microstrip filter using a full mapping.

## V. CONCLUSIONS

We present a family of robust techniques for exploiting sensitivities in EM-based circuit optimization through SM. We exploit a PSM concept where a reduced set of parameters is sufficient in the PE process. Available gradients can initialize mapping approximations. Exact or approximate Jacobians of responses can be utilized. For flexibility, we propose different possible “mapping matrices” for the PE processes and SM iterations. Finite differences may be used to initialize the mapping. A hybrid approach incorporating the Broyden formula can be used for mapping updates. Our approaches have been tested on several examples. They demonstrate simplicity of implementation, robustness, and do not rely on designer intervention.

Final mappings are useful in statistical analysis and yield optimization. Furthermore, the notion of exploiting reduced sets of physical parameters reflects the importance of the idea of post-production tuning.

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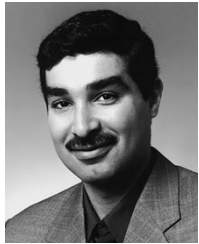
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